

Inference-Proof Materialized Views Doctoral Examination

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Context of this Work

Inference-Proof Data Publishing

Nowadays: Data publishing is ubiquitous

- Governments and companies provide data
- People share data about their private lives

But: Original data often contains sensitive (personal) information

- Set up a confidentiality policy
- Release "secure views" instead of original data
 - Do not reveal any confidential information
 - Consider adversary's abilities to infer information

Framework and Goal

Framework: Relational model relying on first-order logic

- Complete original instance r (definite knowledge: +/-)
- Confidentiality policy *psec* of potential secrets (∃X) R(X, c) s.t. each variable X occurs only once
- Adversary is aware of policy and protection mechanism

Goal: Enforce policy **efficiently** by weakened view on r s.t.

- ▶ Weakened view weak(r, psec) contains only true knowledge
- Inference-proofness from adversary's point of view: For each $\Psi \in psec$ there is a "secure" alternative instance r^{Ψ}
 - r^{Ψ} does **not satisfy** Ψ
 - r^{Ψ} is **indistinguishable** from original instance r

$$ightarrow$$
 weak $(r^{\Psi}, psec) =$ weak $(r, psec)$



Confidentiality by Weakening



Construction of Weakened Views

Stage 1: Disjoint disjunction templates (independent of r)

- Partition the policy *psec* into disjoint clusters C₁,..., C_q (inducing disjunction templates) of a certain minimum size
- If necessary: Construct additional potential secrets

Stage 2: Weakened view weak(r, psec) (dependent on r)

- Keep each tuple of r not satisfying any $\Psi \in C_i$
- ▶ Introduce each disjunction $\bigvee_{\Psi \in C_i} \Psi$ satisfied by r
- Knowledge not satisfying kept tuples or disjuncts is negative
- \rightarrow Three classes of knowledge: +, V, –

Inference-Proofness by Isolation

Structure of weakened views:

+
$$R(\boldsymbol{c}_{1}), R(\boldsymbol{c}_{2}), \ldots, R(\boldsymbol{c}_{p})$$
 (definite knowl.)
 $\downarrow R(\boldsymbol{c}_{i}) \not\models_{DB} \Psi_{j,\ell}$
 $\lor \Psi_{1,1} \lor \ldots \lor \Psi_{1,k_{1}} \ldots \Psi_{m,1} \lor \ldots \lor \Psi_{m,k_{m}}$
 $\downarrow \Psi_{i,j} \not\models_{DB} \Psi_{\overline{i},\overline{j}}$
 $\neg R(\boldsymbol{d}_{i}) \not\models_{DB} \neg \Psi_{j,\ell}$
- $\neg R(\boldsymbol{d}_{1}), \neg R(\boldsymbol{d}_{2}), \neg R(\boldsymbol{d}_{3}), \ldots$ (definite knowl.)

Hence: For each $\Psi \in \Psi_{i,1} \vee \ldots \vee \Psi_{i,k_i}$ alternative instance r^{Ψ} with

r^Ψ ⊭_M Ψ ✓ (but: r^Ψ ⊨_M Ψ_{i,1} ∨ ... ∨ Ψ_{i,ki})
 r^Ψ ⊨_M +, ∨, - → indistinguishability by construction of weakened views ✓



About the Clustering of Policy Elements

Desired properties for disjoint disjunction templates

- ► Credibility of all disjuncts ~→ confidentiality
- ► Semantically meaningful ~→ availability
- ► Certain length ~→ level of confidentiality/availability

Desired properties for disjoint clustering of policy elements

- Consider (high-level) specification of admissible clusters
 Depends on application scenario
- Each cluster must have a certain (minimum) size k*
- Minimize number of additional potential secrets

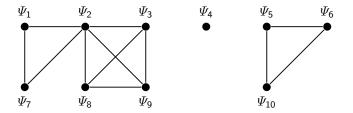
Clustering problem is NP-hard for $k^* \ge 3$ (Reduction of X3C)

Efficient Clustering for $k^* = 2$ (1)

Model all admissible clusters within simple and undirected **Indistinguishability Graph** G = (V, E) with

•
$$V := \{ \Psi \in psec \mid \Psi \text{ is to be clustered} \}$$

•
$$E := \{ \{ \Psi, \Psi' \} \mid \Psi \lor \Psi' \text{ is admissible} \}$$

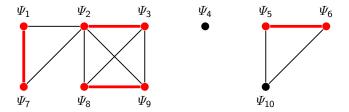




Efficient Clustering for $k^* = 2$ (2)

Compute maximum matching on indistinguishability graph

- Matching: Subset of pairwise vertex-disjoint edges
- Induces set of disjoint and admissible disjunction templates

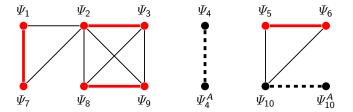




Efficient Clustering for $k^* = 2$ (3)

How to handle policy elements not covered by the matching?

- Pair with additional (artificial) potential secrets
- Minimum number of these due to maximum matching



Inference-Proof Materialized Views



Inference-Proofness under A Priori Knowledge



(already known)

Introducing A Priori Knowledge

Usually: Adversary also has some a priori knowledge prior

Challenge for inference-proofness: "secure" alternative instance r^{Ψ}

- r^Ψ does not satisfy Ψ
 r^Ψ is indistinguishable from original r
- \blacktriangleright r^{Ψ} satisfies prior

Assumed prior: "Single Premise TGDs" of the form

$$\Gamma := (\forall \boldsymbol{X}) [R(\boldsymbol{X}, \boldsymbol{c}_1) \Rightarrow (\exists \boldsymbol{Y}) R(\boldsymbol{X}, \boldsymbol{Y}, \boldsymbol{c}_2)] \quad \text{s.t.}$$

- each X occurs only once in $prem(\Gamma)$ and
- each X, Y occurs only once in $concl(\Gamma)$

Confidentiality Compromising Dependencies

Semantics of Single Premise TGDs: (also via transitive chains)

- Existent DB-Tuple \Rightarrow Existence of other DB-Tuple
- ▶ Non-Existent DB-Tuple ⇒ Non-Existence of other DB-Tuple

Broken isolation in weakened views:

+
$$R(\boldsymbol{c}_1), R(\boldsymbol{c}_2), \ldots, R(\boldsymbol{c}_p)$$
 (definite knowl.)

 $\forall Pependencies$
 $\forall \Psi_{1,1} \lor \ldots \lor \Psi_{1,k_1} \ldots \Psi_{m,1} \lor \ldots \lor \Psi_{m,k_m}$ Dependencies

 $\bullet Dependencies$
- $\neg R(\boldsymbol{d}_1), \neg R(\boldsymbol{d}_2), \neg R(\boldsymbol{d}_3), \ldots$ (definite knowl.)

Inference-Proof Materialized Views
Inference-Proofness under A Priori Knowledge
Disabling Harmful Inference-Channels

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Re-Establishing Sufficient Isolation (1)

Handling of dependency \varGamma interfering with policy elements

- Add policy elements protecting prem(Γ) and concl(Γ)
 → Do not reveal satisfaction-status of premise or conclusion
- ► Attention: New policy elements ~→ further interferences

Problem: Disjunctions do not always guarantee distortion of non-satisfaction of conclusions

Only escape: Resort to distortion by complete refusal

Inference-Proof Materialized Views
Inference-Proofness under A Priori Knowledge
Disabling Harmful Inference-Channels

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Re-Establishing Sufficient Isolation (2)

Inference-channel within disjunctive knowledge:

How to eliminate this kind of inference-channel?

- Partitioning of *prior* s.t. Γ_1 and Γ_2 in same partition, if
 - ▶ their conclusions imply the same Ψ (under some σ_1, σ_2) or
 - they can possibly form a transitive chain
- Do not construct disjunction, if all disjuncts imply a premise of the same partition



Conclusion & Future Work

Conclusion & Future Work

Main contributions:

- Confidentiality by cooperative weakening without lies
- Even if adversary employs Single Premise TGDs
- Efficient computation for disjunctions of length $k^* = 2$
- ▶ Without prior: Confidentiality level can provably be varied

Possible future work:

- Clustering algorithm for $k^* \ge 3 \quad (\rightarrow \text{Reasonable heuristic})$
- More expressive classes of a priori knowledge
- Proof for different levels of confidentiality under prior
- ▶ Model *k*-anonymity/ℓ-diversity within weakening approach



Backup Slides

Confidentiality by Weakening: Example (1)

Policy:
$$psec = \{ \Psi_1 = R(a, b, c), \Psi_2 = R(a, b, d) \}$$

Complete original instance r:

$$\begin{array}{c|ccc} + & - & R(a,b,c), R(a,c,c), R(b,a,c) \\ \hline (a,b,c) & (a,a,a) & (\forall X)(\forall Y)(\forall Z) \ [& (X \equiv a \land Y \equiv b \land Z \equiv c) \lor \\ (a,b,d) & (X \equiv b \land Y \equiv c \land Z \equiv c) \lor \\ \hline \vdots & \neg R(X,Y,Z) &] \end{array}$$

Obviously: r satisfies $\Psi_1 \quad (\rightarrow \text{ to be weakened})$

Confidentiality by Weakening: Example (2) Disjunction template: $\Psi_1 \lor \Psi_2 = R(a, b, c) \lor R(a, b, d)$

Weakened view weak(r, psec):

+	-	
(a, b, c)	(a, a, a)	
(a, c, c)	(a, a, b)	
(b, a, c)	÷	\implies
	(a, b, d)	,
	÷	

Disjunctive knowledge: $R(a, b, c) \lor R(a, b, d)$

$$R(a, c, c), R(b, a, c)$$

$$R(a, b, c) \lor R(a, b, d)$$

$$(\forall X)(\forall Y)(\forall Z) [$$

$$(X \equiv a \land Y \equiv b \land Z \equiv c) \lor$$

$$(X \equiv a \land Y \equiv c \land Z \equiv c) \lor$$

$$(X \equiv b \land Y \equiv a \land Z \equiv c) \lor$$

$$\neg R(X, Y, Z)]$$

Achievement: weak (r, psec) does **neither** imply Ψ_1 **nor** Ψ_2

Isolation within Disjunctive Knowledge

Policy of only ground atoms: Isolation due to disjoint clustering

But: Existential quantification in policy can break up isolation

- Consider: $\Psi_1 \lor \Psi_2$ with $\Psi_1 \models_{DB} \Psi_2$
- ▶ Then: $\Psi_1 \lor \Psi_2 \models_{DB} \Psi_2$ reveals validity of Ψ_2 *f*
- Also harmful, if Ψ_1 and Ψ_2 stem from different disjunctions

How to re-establish isolation?

- ► Only weakest sentences of *psec* may occur in disjunctions → No implication between disjuncts
- Stronger policy elements still implicitly protected

Experimental Evaluation for $k^* = 2$

About the prototype implementation

- Criterion for admissible disjunctions: "Interchangeability"
- "Boost"-library for maximum matchings on general graphs

Lessons learned from 5 experiment setups

- Algorithm efficiently handles input instances of realistic size
- Size and structure of psec and prior crucial for runtime
- Low number of additional potential secrets and refusals
 But: Admissibility criterion should fit to application scenario
- Parallelization: Doubling threads nearly halves runtime
- Clustering is significantly faster with matching heuristic
 Only slight loss of availability